Effects Beyond Center-of-Mass Separability in a Trapped Bosonic Mixture: Exact Results

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The properties of trapped Bose-Einstein condensates (BECs) at the limit of an infinite number of particles draw much attention [1-12]. There are rigorous results for the ground state and, under some conditions, on the dynamics with time-independent Hamiltonians. In the first part of the work, generalizations to time-periodic (Floquet) many-boson systems are presented. To this end, a solvable many-body model of a generic driven mixture of trapped BECs is devised, and its properties are investigated. In particular, we show that the quasi-energy per particle computed at the limit of an infinite number of particles does not coincide with the mean-field value at this limit unless the relative center-of-mass coordinate of the two BECs is not activated by the driving forces [13]. In the second part of the work, an application is discussed. We investigate the imprinting of angular momentum and its fluctuations when steering a BEC by driving an interacting bosonic impurity embedded in it, and the resulting modes of rotations [13]. Finally, in the third part of the work, a static solvable many-body model with center-of-mass inseparability is introduced, and the combined effects of interactions and trapping on the energy, system's stability, densities, condensation of intra-species and separability of inter-species reduced density matrices, as well the position—momentum uncertainty product, are elucidated [14].

References

- [1] Y Castin and R Dum, Phys. Rev. A 57, 3008 (1998)
- [2] E H Lieb, R Seiringer and J Yngvason, Phys. Rev. A **61**, 043602 (2000)
- [3] E H Lieb and R Seiringer, Phys. Rev. Lett. 88, 170409 (2002)
- [4] L Erdős, B Schlein and H-T Yau, Phys. Rev. Lett. 98, 040404 (2007)
- [5] L Erdős, B Schlein and H-T Yau, Invent. Math. 167, 515 (2007)
- [6] S Klaiman and O E Alon, Phys. Rev. A **91**, 063613 (2015)
- [7] S Klaiman, A I Streltsov and O E Alon, Phys. Rev. A 93, 023605 (2016)
- [8] S Klaiman and L S Cederbaum, Phys. Rev. A 94, 063648 (2016)
- [9] I Anapolitanos, M Hott and D Hundertmark, Rev. Math. Phys. 29, 1750022 (2017)
- [10] A Michelangeli and A Olgiati, Anal. Math. Phys. 7, 377 (2017)
- [11] O E Alon, J. Phys. A **50**, 295002 (2017)
- [12] L S Cederbaum, Phys. Rev. A **96**, 013615 (2017)
- [13] O E Alon, Entropy **22**, 1342 (2020)
- [14] O E Alon and L S Cederabum, to be submitted